


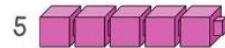
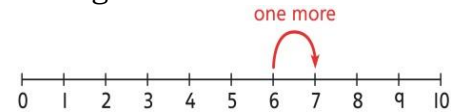
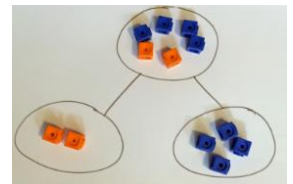
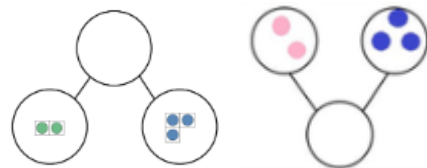
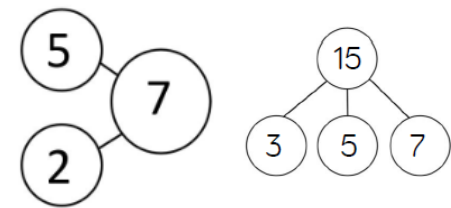


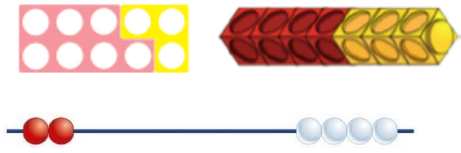
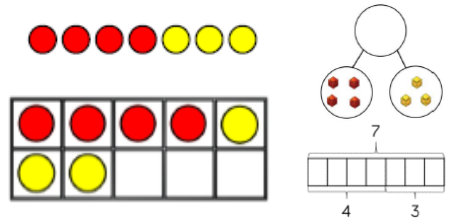
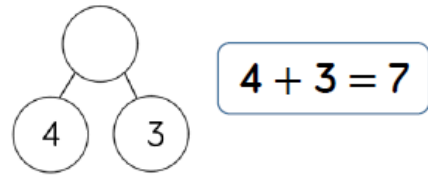
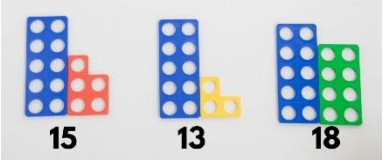
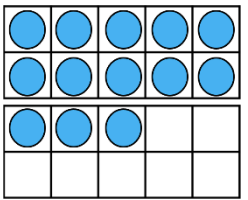
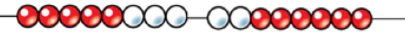
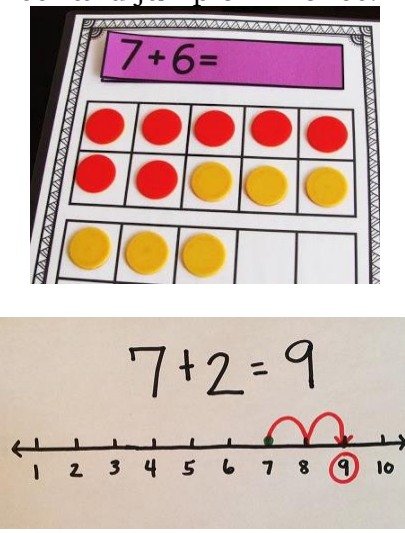
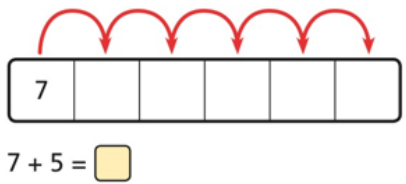




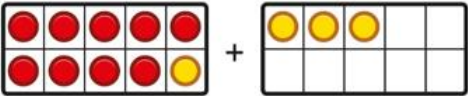
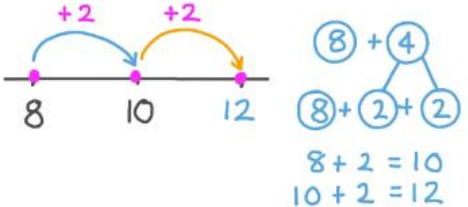
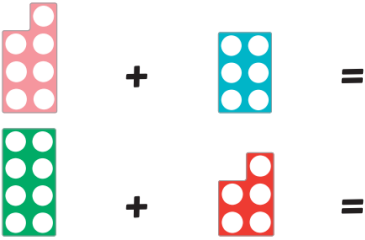

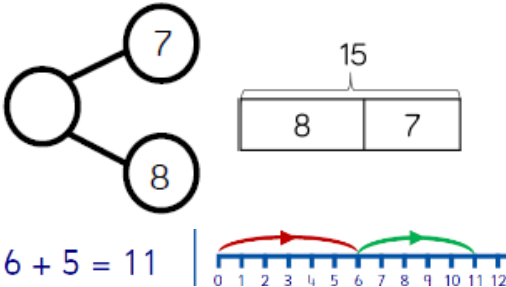
Calculation Policy – Progression in Calculations

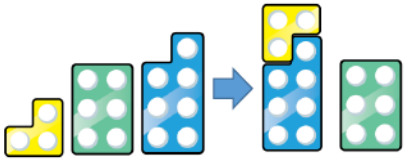
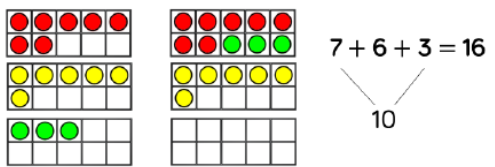
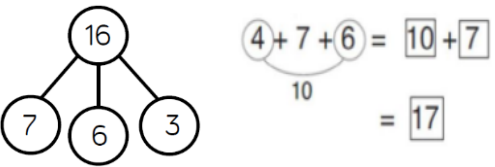
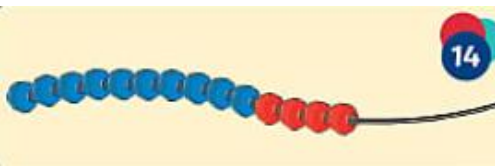
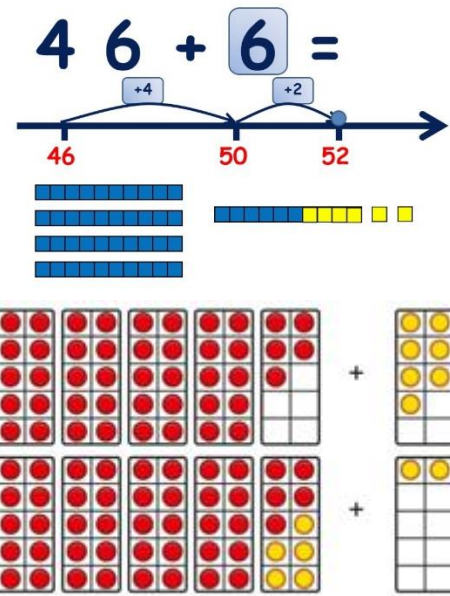


Progression in Calculations - Addition

Expected Year Group	Objectives	Concrete	Pictorial	Abstract
EYFS	Find 1 more than/find 1 less than	<p>Children add one more person or object to a group to find one more or take away one object to find one less.</p> 	<p>Children add one more cube or counter to a group to represent one more.</p>  <p>Children take away one cube or counter from a group to represent one less.</p> <p>Daniel has 6 blocks.</p>  <p>He takes one away. There are 5 blocks left.</p>  <p>5 is one less than 6.</p> <p>They could then use squares in their book to represent this.</p>	<p>Use a number line to understand how to link counting on with finding one more.</p> 
Year 1	Understand part/whole relationship	<p>Sort a set of people or objects into parts and understand their relationship within the whole.</p> 	<p>Draw pictures to represent the parts and their relationship within the whole.</p> 	<p>Use a part-whole model to represent numbers.</p> 

Year 1	Add 1-digit numbers within 10	<p>Using apparatus such as cubes, bead strings and Numicon to add two groups together and break apart again.</p> 	<p>Use five and ten frames, bar models or part whole models to represent key number bonds.</p> 	<p>Use of models alongside written calculation.</p> 
Year 1	Understanding teen numbers as a complete 10 plus more ones	<p>Make groups of 10 and then count the extra ones.</p> 	<p>Use a ten frame to support finding complete sets of 10 and count the extra ones.</p> 	<p>Number sentences to show $10 + ? = ?$</p> <p>1 ten plus 3 ones equals 13. $10 + 3 = 13$</p>
Year 1	Adding by starting at the bigger number and counting on	<p>Use a bead string to make the start number and then count on in ones.</p>  <p>$8 + 7 = 15$</p>	<p>Use a pictorial representation to show making the larger number first and counting on or use a number line to start at the larger number and jump on in ones.</p> 	<p>Use number lines or number tracks to support counting on.</p>  <p>$7 + 5 = \square$</p>



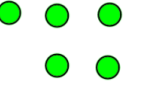
Year 1	Bridging the 10 using number bonds (regrouping to make 10)	<p>Use bead strings or cubes to add on to make 10 first and then count on what is leftover.</p>  <p>Complete $7 + 5$ by starting at 7 and counting on 3 to make 10 then add on the additional 2 to make 12.</p>  <p>Complete $6 + 5$ by starting at 6 and counting on 4 to make 10 then add on the additional 1 to make 11.</p>	<p>Use pictures of tens frames or a number line to regroup or partition the smaller number using the part-part-whole model to make 10.</p>  <p>$9 + 4$ can be shown as $9 + 1 + 3$</p> 	<p>Use a number line or number track to support the calculation if needed.</p> <p>$7 + 4 = 11$</p> <p>If I am at seven, how many more do I need to make 10? (3) How many more do I add on now? (1)</p>
Year 1/2	Add 1 and 2-digit numbers to 20	<p>Use apparatus to support counting on.</p>  	<p>Pictorial representations to support adding within 20.</p>  <p>$6 + 5 = 11$</p>	<p>Use of number sentences supported by number lines/number tracks where needed.</p> <p>$8 + 7 = 15$</p>

Year 2	Add three 1-digit numbers	<p>Use manipulatives to look for number bonds to 10 or doubles to add the numbers more efficiently.</p> 	<p>Use pictorial representations to look for number bonds to 10 or doubles to add the numbers more efficiently.</p> 	<p>Use part-whole models to support answering of number sentences if required. Children looking for the most efficient method/order to complete the calculation.</p> 
Year 2	Adding a 2-digit number and ones (bridging the ten)	<p>Use bead strings or cubes to add on to make 10 first and then count on what is leftover.</p>  <p>Complete $14 + 8$ by starting at 14 and counting on 6 to make 20 then add on the additional 2 to make 22.</p>	<p>Use Base-10 or tens frames or a number line to regroup or partition the smaller number to make the closest multiple of 10 first then count on.</p> 	<p>Use a number line or number track to support the calculation if needed.</p> <p>$27 + 8 = 35$</p> <p>If I am at twenty seven, how many more do I need to make the next ten? (3) How many more do I add on now? (5)</p>

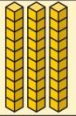


Year 2

Introducing columns:
 Adding a 1-digit number to a 2-digit number (not bridging a 10)

Place counters on a place value grid to aid addition.

Tens	Ones
	
	

Using Base-10 tens and ones on a place value grid.

T	O
	
	





Using digits set out vertically in columns.



	T	O
	3	4
+		5
		9

Year 2

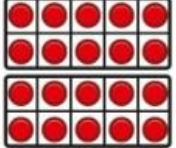



Introducing columns:
 Adding a 1-digit number to a 2-digit number using exchange

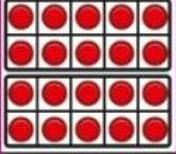


Exchange 10 ones for 1 ten.

T	O
	
	

T	O
	
	

Exchange 10 ones for 1 ten.


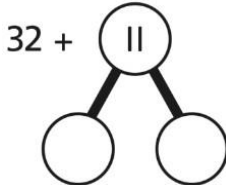
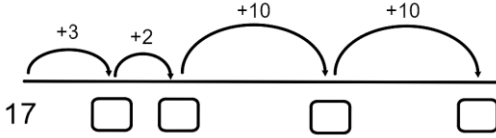
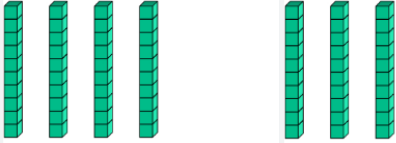
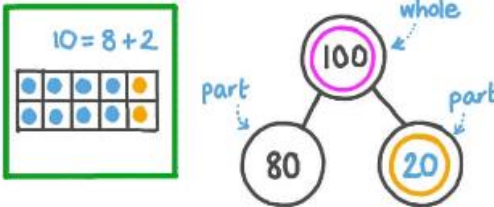

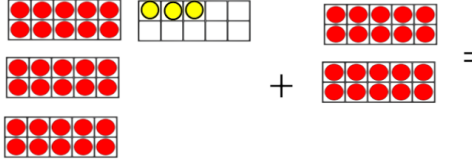
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






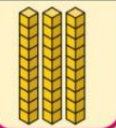


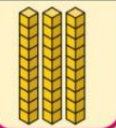





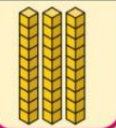













































T	O
	
	

Exchange 10 ones for 1 ten.

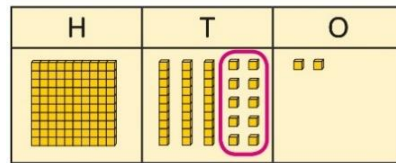
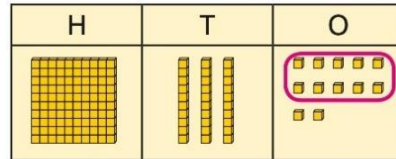
	T	O
	2	4
+		8
		2
	3	

	T	O
	2	4
		8
	3	2

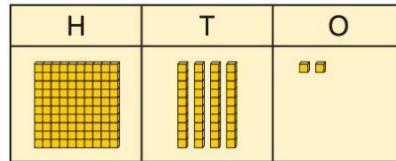
Year 2	Adding two 2-digit numbers	<p>Add the 10s and 1s individually (always start with 1s).</p>  <p>$4 + 3 = 7$ There are 7 ones in total.</p> <p>$3 + 2 = 5$ There are 5 tens in total.</p> <p>$34 + 23 = 57$</p>	<p>Add the 10s and 1s individually. Use a part-whole model to support.</p>  <p>$11 = 10 + 1$</p> <p>$32 + 1 = 33$ $33 + 10 = 43$</p> <p>$32 + 11 = 43$</p>	<p>Add the 10s and the 1s individually, bridging 10s where required. A number line can support the calculations.</p>  $\begin{array}{r} \text{T} \text{ O} \\ 17 \\ + 25 \\ \hline \end{array}$
Year 2	Adding multiples of 10	<p>Use known number bonds to apply to adding tens.</p>  <p>$4 + 3 = 7$. So, 4 tens add 3 tens must be 7 tens which is 70.</p>	<p>Use part-whole models or tens frames to support adding multiples of 10.</p>  <p>$100 = 80 + 20$</p>	<p>Use known number bonds to apply to adding tens.</p> <p>$5 + 2 = 7$ So, $50 + 20 = 70$</p>
Year 2	Adding a 2-digit number and multiples of 10	<p>Add the tens and then re-group.</p>  <p>32 is 3 tens and 2 ones. 20 is 2 tens.</p> <p>There are 5 tens in total and 2 ones. So, $32 + 20$ is 52.</p>	<p>Add the tens and then re-group.</p>  <p>$30 + 20 = 50$ $50 + 3 = 53$</p>	<p>Add the tens and then re-group.</p> <p>$57 + 30 = ?$</p> <p>$50 + 30 = 80$ $80 + 7 = 87$</p> <p>$57 + 30 = 87$</p>

Year 2	Introducing columns: Adding a 2-digit number and multiples of 10	Add the tens using a place value grid to support. <table><tr><th>T</th><th>O</th></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table>	T	O					Add the tens using a place value grid to support. <table><tr><th>T</th><th>O</th></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table>	T	O					Use vertical columns to add the tens. <table><tr><th>T</th><th>O</th></tr><tr><td>1</td><td>6</td></tr><tr><td>3</td><td>0</td></tr><tr><td>4</td><td>6</td></tr></table>	T	O	1	6	3	0	4	6																																																				
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Year 3	Add a three-digit number and ones	<p>No exchanging required:</p> <table><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td><td></td></tr><tr><td>+</td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr></table> <p>Exchanging required: 1)</p> <table><tr><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr></table> <table><tr><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td></td><td></td></tr></table>	Hundreds	Tens	Ones				+						H	T	O							H	T	O				<p>No exchanging required:</p> <table><tr><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td></td><td></td></tr><tr><td>3</td><td>4</td><td>8</td></tr></table> <p>Exchanging required:</p> <table><tr><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td></td><td></td></tr><tr><td>3</td><td>5</td><td>2</td></tr></table>	H	T	O				3	4	8	H	T	O				3	5	2	<p>Use vertical columns to aid addition. No exchanging required:</p> <table><tr><th>H</th><th>T</th><th>O</th></tr><tr><td>3</td><td>5</td><td>3</td></tr><tr><td>+</td><td></td><td>6</td></tr><tr><td></td><td></td><td></td></tr></table> <p>Exchanging required:</p> <table><tr><th>H</th><th>T</th><th>O</th></tr><tr><td>3</td><td>5</td><td>5</td></tr><tr><td>+</td><td></td><td>6</td></tr><tr><td></td><td></td><td>1</td></tr><tr><td></td><td>1</td><td></td></tr></table>	H	T	O	3	5	3	+		6				H	T	O	3	5	5	+		6			1		1	
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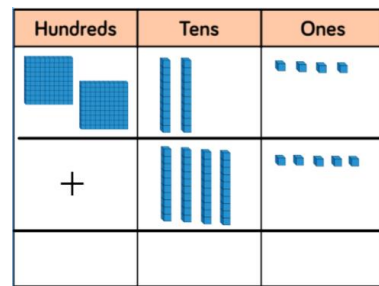
3)



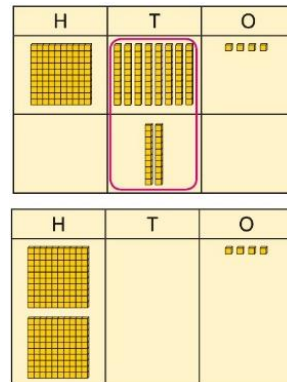
Year 3

Add a three-digit number and tens

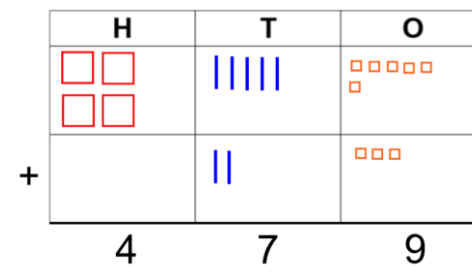
No exchanging required:



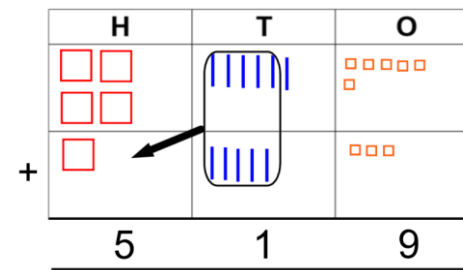
Exchanging required:



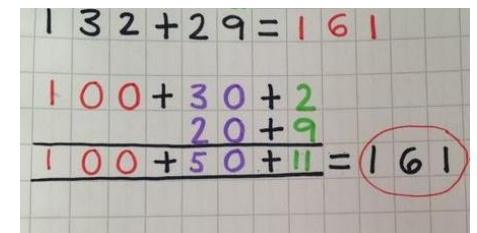
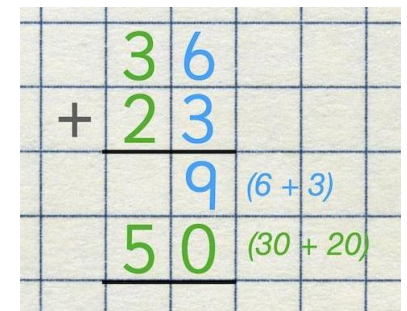
No exchanging required:



Exchanging required:



Expanded Partitioning Method:



Year 3

Add a three-digit number and hundreds

No exchanging required:

Hundreds	Tens	Ones
+		

Exchanging required:

H	T	O

No exchanging required:

H	T	O
+		
7	8	8

Exchanging required:

H	T	O
+		
7	9	1

Expanded Partitioning Method:

This is set out vertically, in a similar fashion to the traditional form of addition.

$$\begin{array}{r}
 215 \\
 133 + \\
 \hline
 8 \text{ (5 + 3)} \\
 40 \text{ (10 + 30)} \\
 300 \text{ (200 + 100)} \\
 \hline
 348
 \end{array}$$

$$\begin{array}{r}
 300 + 60 + 7 \\
 + 100 + 40 + 8 \\
 \hline
 400 + 100 + 17 = 517
 \end{array}$$

Formal Column Method (no exchanging):

$$\begin{array}{r}
 215 \\
 + 133 \\
 \hline
 348
 \end{array}$$

$$\begin{array}{l}
 5 \text{ (ones)} + 3 \text{ (ones)} = 8 \text{ ones} \\
 1 \text{ (ten)} + 3 \text{ (tens)} = 4 \text{ tens} \\
 2 \text{ (hundreds)} + 1 \text{ (hundred)} = 3 \text{ (hundreds)}
 \end{array}$$

Formal Column Method
(exchanging required):

$$\begin{array}{r} 226 \\ + 193 \\ \hline 419 \\ 1 \end{array}$$

Start with the least significant digits (ones) $6 + 3 = 9$.
Add the tens ($2 + 9 = 11$). Because the answer is a two digit number, it has to be exchanged.
Add the hundreds ($2 + 1 = 3$, + the '1' being exchanged = 4)

Year 4

Add numbers with up to 4 digits

Use place value equipment on a place value grid to support addition.

Th	H	T	O
●	●●●●●●●●		●●●●●●●●
	●●●●●●●●	●●●●●●●●	●●●●●●●●

Draw a pictorial representation of the columns and place value counters to further support addition particularly where exchanging is required.

Th	H	T	O
1000 1000 1000 1000 1000	100 100 100 100	10 10 10 10 10 10	1 1 1 1 1 1 1 1 1 1
8	8	0	2

Use the formal column method to add (including exchanges).

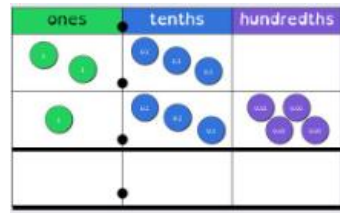
Th	H	T	O
	5	5	4
+ 4	2	3	7
<hr/>			
		9	1

Th	H	T	O
	5	5	4
+ 4	2	3	7
<hr/>			
		9	1

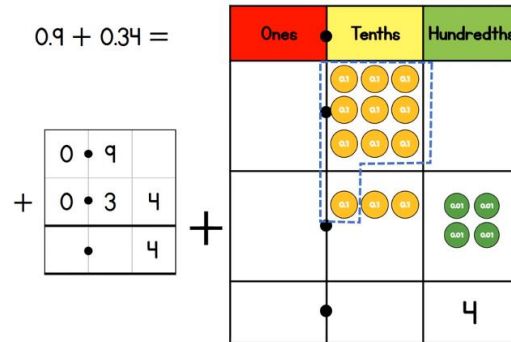
Year 4

<p>Add decimals with 2 decimal places, including money.</p>

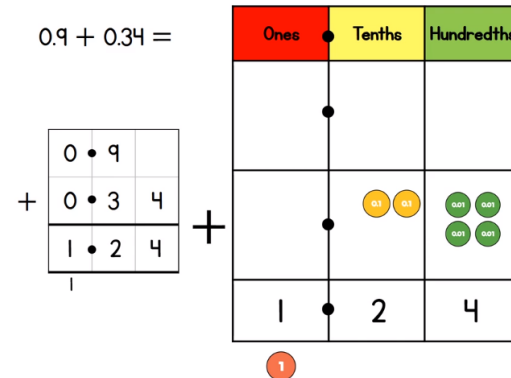
Introduce decimal place value counters and model how to exchange for addition.



$0.9 + 0.34 =$

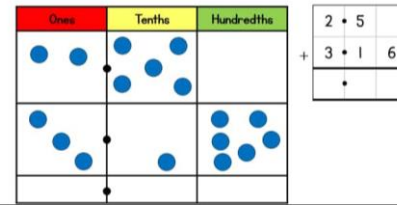


$0.9 + 0.34 =$



Pictorial representations of a decimal place value grid.

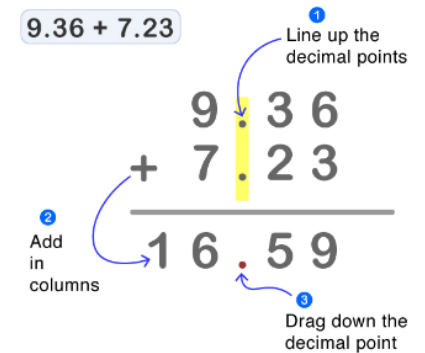
$$2.5 + 3.16 =$$



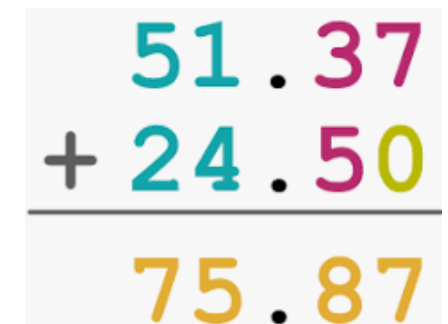
Adapt the formal column method for use with decimal numbers. Line digits up according to place value.

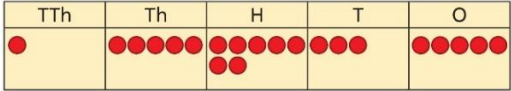
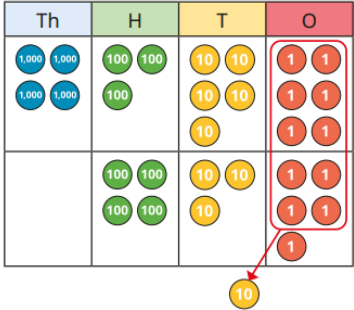
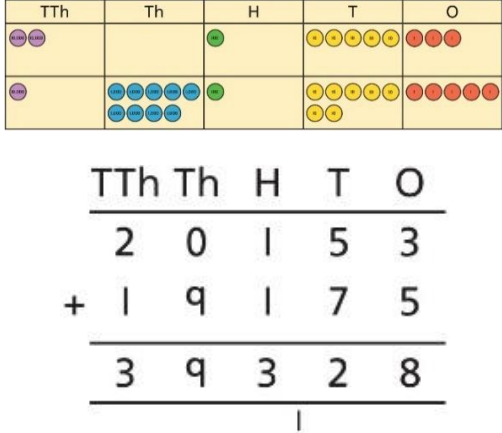
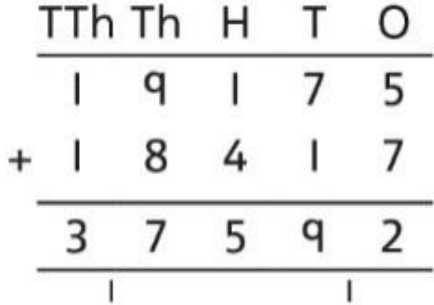
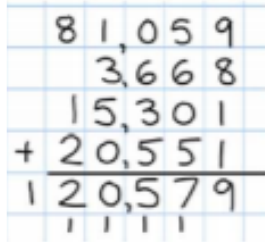


$9.36 + 7.23$



Where decimals have a different number of digits after the decimal point, insert a zero in the gap as a place holder.



Year 5/6	<p>Add numbers with more than 4 digits</p>	<p>Use place value equipment to support additions.</p>  <p>Add a row of counters onto the place value grid to show 15,735 + 3,024.</p> <p>Continue to use concrete apparatus to reinforce the idea of exchanging with higher numbers.</p> 	<p>Use place value equipment alongside written methods.</p> 	<p>Use of formal column addition, including exchanging.</p> 
Year 5	<p>Add numbers with up to 3 decimal places</p>	<p>Use strategies from year 4 but adapt for longer/more varied decimal numbers.</p>	<p>Use strategies from year 4 but adapt for longer/more varied decimal numbers.</p>	<p>Use strategies from year 4 but adapt for longer/more varied decimal numbers.</p>
Year 6	<p>Add several numbers of increasing complexity, including adding money, measure and decimals with different numbers of decimal points.</p>			<p>Adapt the formal written method previously used to include several numbers.</p> 

For unlike decimals, line up the decimal points and insert a zero in the gap as a place holder.

$$\begin{array}{r} 23.361 \\ 9.080 \\ 59.770 \\ + 1.300 \\ \hline 93.511 \\ 212 \end{array}$$